2.10 Illustrate the following equations using circuits of switches:

(a)
$$XY + XY' = X$$

(b)
$$(X + Y')Y = XY$$

2.11 Simplify each of the following expressions by applying *one* of the theorems. State the theorem used.

(a)
$$(A' + B' + C)(A' + B' + C)'$$

(b)
$$AB(C' + D) + B(C' + D)$$

(c)
$$AB + (C' + D)(AB)'$$

(d)
$$(A'BF + CD')(A'BF + CEG)$$

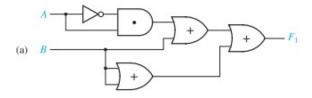
2.12 Simplify each of the following expressions by applying *one* of the theorems. State the theorem used.

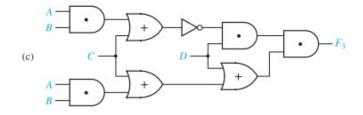
(a)
$$(X + Y'Z) + (X + Y'Z)'$$

(b)
$$[W + X'(Y + Z)][W' + X'(Y + Z)]$$

(c)
$$(V'W + UX)'(UX + Y + Z + V'W)$$

2.13 For each of the following circuits, find the output and design a simpler circuit that has the same output. (*Hint:* Find the circuit output by first finding the output of each gate, going from left to right, and simplifying as you go).





2.14 Draw a circuit that uses only one AND gate and one OR gate to realize each of the following functions:

(b)
$$(V + W + Y + Z)(U + W + Y + Z)(W + X + Y + Z)$$

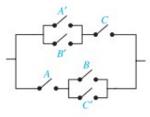
2.15 Use only DeMorgan's relationships and Involution to find the complements of the following functions:

(a)
$$f(A, B, C, D) = [A + (BCD)'][(AD)' + B(C' + A)]$$

2.16 Using just the definition of the dual of a Boolean algebra expression, find the duals of the following expressions:

(a)
$$f(A, B, C, D) = [A + (BCD)'][(AD)' + B(C' + A)]$$

- 2.17 For the following switching circuit, find the logic function expression describing the circuit by the three methods indicated, simplify each expression, and show they are equal.
 - (a) subdividing it into series and parallel connections of subcircuits until single switches are obtained
 - (b) finding all paths through the circuit (sometimes called tie sets), forming an AND term for each path and ORing the AND terms together
 - (c) finding all ways of breaking all paths through the circuit (sometimes called cut sets), forming an OR term for each cut set and ANDing the OR terms together.



- 2.18 For each of the following Boolean (or switching) algebra expressions, indicate which, if any, of the following terms describe the expression: product term, sum-of-products, sum term, and product-of-sums. (More than one may apply.)
 - (a) X'Y

- (b) XY' + YZ
- (c) (X' + Y)(WX + Z)
- (d) X + Z