

# Directional Routing over Orthogonal Lines: A Performance Evaluation

## Invited Paper

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**Abstract**—Routing in wireless ad-hoc networks have had to grapple with the twin requirements of connectivity and scalability. Recently, [1] has attempted to mitigate this issue by using directional communication methods to find intersections between source-rendezvous and rendezvous-destination paths, providing effective routing in unstructured, flat networks. [1] showed that by “drawing” two lines orthogonal to each other at each node, it is possible to provide over 98% connectivity while maintaining only order  $O(N^{3/2})$  states. It is interesting, however to investigate what happens when additional lines are “drawn” and how that affects connectivity, path length, state complexity, control packet overhead, and aggregate throughput. In this paper, we examine how transmitting along one, two, three, and four lines affects routing and provide both analytical bounds for connectivity as well as packetized simulations on how these methods stack up in a more realistic environment. We show that by sending packets out in more directions, increased connectivity and smaller average path length results only up to a point. The trade-off, however, is added state information maintained at each node. We also show that in mobile environments, adding additional lines increases the chances for successful packet delivery only marginally.<sup>1</sup>

### I. INTRODUCTION

Routing in wireless ad-hoc networks have had to grapple with the twin requirements of connectivity and scalability. Early MANET protocols such as DSR [9], DSDV [7], AODV [8], among others, explored proactive and reactive routing methods which either flooded information during route dissemination or during route discovery respectively. While effective in providing high connectivity, as networks grow, however, flooding poses an obvious scalability problem. In response, several topology-based routing protocols such as OLSR [10], Hierarchical Routing [11], among others, have implemented limited flooding techniques to disseminate route information. Additionally, position-based routing paradigms such as GPSR [4] were also proposed to reduce the state complexity and control-traffic overhead by leveraging the Euclidean properties of a coordinate space embedding. These schemes require nodes

to be assigned a coordinate in the system, and still require a mapping from nodeID to coordinate location.



Fig. 1. Wireless directional communications methods such as directional antennas and free-space-optical transceivers have become increasingly available.

In effort to increase bandwidth on wireless transmissions, researchers in recent years have been investigating free space optical (FSO) communications technologies as a supplement to traditional RF methods. Currently available in point-to-point links in terrestrial last mile applications and in infrared indoor LANs [24] [23], FSO has several attractive characteristics like (i) *dense spatial reuse*, (ii) *low power usage per transmitted bit*, (iii) *license-free band of operation*, and (iv) *relatively high bandwidth compared to RF*. Conversely, FSO suffers from (i) *the need for line of sight (LOS) alignment between nodes* and (ii) *reduced transmission quality in adverse weather conditions*. [15] proposed several ways to mitigate these issues by tessellating low cost FSO transceivers in a spherical fashion (see Figure 1) and replacing long-haul point-to-point links with short, multi-hop transmissions.

As reliable multi-hop FSO communication becomes more of a reality, it becomes increasingly important to understand how to deal with and efficiently utilize the directional nature of FSO communications. Because a recent trend in wireless communications has been the desire to leverage directional forms of communications (e.g. directional smart antennas [13] [12]) for more efficient medium usage [12] [13] [14], routing [1], [3] and scalability, prior work has laid much of the foundations for extending directional communications to FSO.

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Recently, [1] has attempted to mitigate the issues of connectivity and scalability by using directional communication methods to find intersections between source-rendezvous and rendezvous-destination paths, providing effective routing in unstructured, fixed, flat mesh networks. [1] showed that by “drawing” two lines orthogonal to each other at each node, it is possible to provide over 98% connectivity while maintaining only order  $O(N^{3/2})$  states. It is interesting, however to investigate what happens when additional lines are drawn and how that affects connectivity, path length, state complexity, control packet overhead, and aggregate throughput. In this paper, we examine how communicating along one, two, three, and four lines affect routing and provide both analytical bounds for connectivity as well as packetized simulations on how these methods stack up in a more realistic environment.

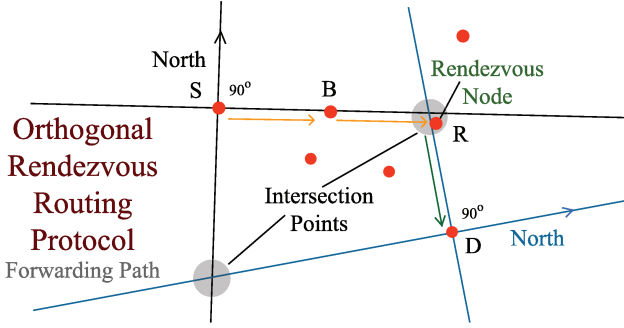


Fig. 2. ORRP Basic Example: Source sends packets to Rendezvous node which in turn forwards to Destination

Specifically, we will show that:

- Using the Multiplier Angle Method (MAM) heuristic suggested in [1], even only one line provides a high degree of connectivity in symmetric topologies as compared to our analytical bounds without MAM.
- In non symmetric topologies (e.g. rectangular) and using the Multiplier Angle Method (MAM) heuristic suggested in [1], increasing the number of lines yields better reach probability and average path lengths.
- Addition of lines yields significantly *diminishing returns* from a connectivity-state maintenance perspective.
- Addition of lines yields better paths from source to destination.
- Addition of lines yields better aggregate throughput overall.
- Increasing the *number of interfaces* per node yields better results for reachability, average path length, and average throughput up to a certain point that is determined by network density.
- As *number of continuous flows* increase, ORRP with increased lines delivers more packets successfully, uses less control packets, and utilizes the medium much more efficiently resulting in higher throughput network-wide.
- Although not the focus of the paper, as *mobility* is added into the equation, addition of lines yields only *marginally* better delivery successes.

The rest of the paper is organized as follows: Section II

gives a brief introduction of Orthogonal Rendezvous Routing Protocol (ORRP) as well as extensions to the protocol to accommodate routing along additional lines. Section III provides some analysis to find connectivity upper bounds and expected path stretch without perimeter routing. Section IV provide performance evaluations in packetized simulations for each case and finally, section V concludes the paper.

## II. ORTHOGONAL RENDEZVOUS ROUTING PROTOCOL EXTENSIONS

The basic concept behind ORRP is simple: knowing that in 2-D Euclidian space, a pair of orthogonal lines centered at different points will intersect at two points at minimum, rendezvous points can be formed to forward packets as shown in Figure 2. To achieve this, ORRP relies on both a proactive element which makes up the “rendezvous-to-destination” path and a reactive element which builds a “source-to-rendezvous” route on demand. Nodes periodically send ORRP announcement packets in orthogonal directions and at each node along the orthogonal route, the node stores the route to the source of the ORRP announcement and the node it received the announcement from (previous hop). When a source node wishes to send to some destination node that it does not know the path for, it sends out a route request packet (RREQ) in its orthogonal directions and each subsequent node forwards in the opposite direction from which it receives the packet. Once a node containing a path toward the destination receives an RREQ, it sends a route reply packet (RREP) in the reverse direction back to the sender and data transmission begins.

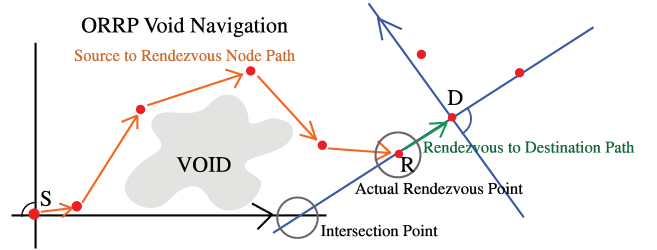


Fig. 3. Traversing voids in sparse networks with differing intersection points

To handle perimeter, void, and path deviation issues, ORRP implemented a Multiplier Angle Method (MAM) heuristic to navigate around voids, perimeters, and maintain relatively straight-line paths for announcement and RREQ packets as shown in Figure 3. [1] showed that ORRP (2 lines) achieves connectivity with high probability even in sparse networks with voids, scales well without imposing GHT-like graph structures [20] (eg: trees, rings, torus etc), maintains a total state information of  $O(N^{3/2})$ , evenly distributed for N-node networks, and does not resort to flooding either in route discovery or dissemination. The price paid by ORRP is suboptimality in terms of path stretch compared to shortest path, but [1] showed that the path stretch is small for generalized networks.

Because MAM allows for even the possibility of sending along one line to also achieve high connectivity (intersections outside of topology region would then be met along the

perimeter), it is interesting to explore the tradeoff between the amount of state maintenance required to achieve similar reach statistics. In the same way, we are interested to see if addition of lines garners significant increases in reachability and better path selection. Extension of ORRP, therefore, is rather straight forward: instead of sending out interfaces that are orthogonal to each other ( $90^\circ$  from each other) as in ORRP, we send out announcement and RREQ packets out interfaces  $180^\circ$  from each other for the “1 line” case,  $60^\circ$  from each other for the “3 line” case, and  $45^\circ$  from each other for the “4 line”. All these cases are compared to the base orthogonal case.

### III. ANALYSIS: REACHABILITY AND PATH STRETCH

Given a Euclidian area over which nodes are scattered, assuming no deviation correction with MAM, a source-destination pair cannot reach each other if all rendezvous points are outside the boundaries of the area. The general idea behind obtaining the reachability upper bound is to find intersections between lines drawn between the source and destination. In cases where all the intersections lie outside of the rectangular area for a particular source and destination oriented in a certain way, our analysis assumes that there is no path from source to destination. Notice that this analysis assumes that probe packets *do not* travel along perimeters of the Euclidian area under consideration and therefore inspects a worst-case upper bound on reachability.

Like in [1], our analysis begins with randomly selecting two source and destination pairs along with random orientations. We then formulate the equations of the lines generated by these two nodes and randomly selected orientations and find their intersection points. The equations of the lines will be different depending on whether we are looking at 1, 2, or 3 lines. If at least one of these intersection points lies in the boundaries of the topology, then we consider that particular source-destination pair as reachable. By iterating through all possible orientations for each possible source-destination pairs, we find a percentage of the total combinations that provide reachability vs. the total paths chosen. Because different Euclidian area shapes will no doubt yield different reachability requirements, we calculated the reachability probability for various area shapes by using Matlab in a grid network. Table I shows the reach probability vs. the number of lines used for calculations.

TABLE I  
COMPARISON OF REACH PROBABILITY VS. NUMBER OF LINES

	1 Line ( $180^\circ$ )	2 Lines ( $90^\circ$ )	3 Lines ( $60^\circ$ )
Circle (Radius 10m)	58.33%	99.75%	100%
Square (10mx10m)	56.51%	98.30%	99.99%
Rectangle (25mx4m)	34.55%	57%	57.61%

It can be seen that the addition of more lines yields significant gains from the one to two line case but only slight gain afterwards. Particular interest is given to the rectangular case where even with three lines, the raw reach probability is very low. We suspect the reason for this is the slim shape yielding to much more path intersections outside of the topology area. [1] showed that most of the unreachable happens at the topology

perimeters and even with additional lines, these perimeter nodes need a very high degree of angular match between lines before a path can be made. The result is that by adding only  $30^\circ$  more to match on, the angle of incidence is still too high to find an intersection within the area.

A similar analysis is done to find path stretch. If a source and destination pair has a line intersection within the topology boundaries, the shortest total distance (from source to intersection point and intersection point to destination) is selected as the path. This distance is divided by the distance between the source and destination to obtain a path stretch. In cases where there is no intersection inside the topology boundaries, we simply add the distance of the perimeter as that is the maximum path we can obtain with MAM. Table II gives the Matlab calculated path stretch for 1, 2, and 3 lines.

TABLE II  
COMPARISON OF PATH STRETCH VS. NUMBER OF LINES

	1 Line ( $180^\circ$ )	2 Lines ( $90^\circ$ )	3 Lines ( $60^\circ$ )
Circle (Radius 10m)	3.854	1.15	1.031
Square (10mx10m)	4.004	1.255	1.039
Rectangle (25mx4m)	4.73	3.24	1.906
Grid (No bounds)	1.323	1.123	1.050

Table I and II show the reachability and path stretch numerical analysis results for 1-3 lines all equidistantly separated from each other. While for reach probability, the affect from one to two lines is dramatic, it can be seen that very little gain is achieved by adding additional lines. In the case of path stretch, however, the addition of additional directions to send announcement and RREQ packets result in much better path selection as more packet interceptions occur. We suspect that in sparser networks or networks with voids, the gains would be negligible as control packets would take similar paths with MAM. It is important to note that with MAM, almost all the corner case reach issues can be resolved with only 2 lines.

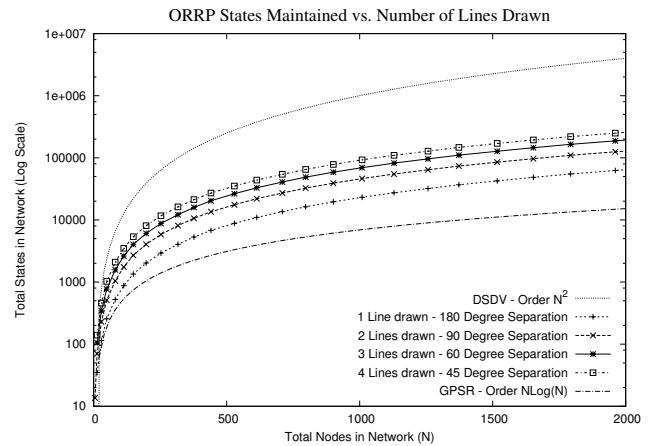


Fig. 4. Total states maintained in network with respect to the number of transmission lines used. As number of lines increase, the number of states maintained throughout network increases.

Figure 4 demonstrates the potential increase in state maintenance needed with the addition of transmission lines. While increasing steadily, it is still much less than order  $N^2$ .

#### IV. PERFORMANCE EVALUATION

In this section, we will evaluate the metrics of *reach probability*, *average path length*, *total state maintenance*, *packet delivery success* and *aggregate throughput* under conditions of varying *network densities*, *number of interfaces*, *network topologies*, *network saturation*, *void conditions*, and *basic random waypoint mobility*. Unless otherwise noted, all simulations were performed using Network Simulator [17]. Interfaces were setup so that they are all aligned equally spaced radially from a single point (the node) with the transmission and receive angle for each interface equal. Adding all the transmission angles together provided for omnidirectional coverage. For example, a node with 24 interfaces would have a transmit/receive and interface separation angle of  $15^\circ$ . In the same way, a node with 4 interfaces would have a transmit/receive and interface separation angle of  $90^\circ$ . Unless otherwise noted, all nodes are outfitted with 24 interfaces and simulation results averaged over 10 runs each under random node orientation.

##### A. Simulation Environment Specifics

Default NS2 simulation parameters are listed in Table III. For evaluating affect of additional lines on various topologies, network voids, and throughput (Sections IV-B-IV-D), 24 interfaces were used as 24 interfaces allowed for evaluating 1-4 lines (needing 2-8 transceivers respectively to send). In Sections IV-B and IV-C, because we were only interested in determining reach probability, average path length, and total states maintained network-wide, it was more important to check the connection from every node in the network to every other node. To do this, each node simply sent a short burst (1-2 CBR packets) to every other node in the network. Reach probability was measured by the number of received vs. sent CBR packets and average path length was calculated by averaging the number of hops from source to destination. In these subsection, total states maintained network-wide were calculated by measuring the size of each routing table (with each entry counted as a single state) *before* any CBR packets are sent and totaling the associated values.

TABLE III  
DEFAULT SIMULATION PARAMETER

Parameter	Values
Transmission Radius	60m
Number of Interfaces	24
TTL for Control Pkts	10
Topology Boundaries	300m x 300m
Announcement Interval	2.0s
Route Timeout	10s
Simulation Time	50s
Mobility	None

Network voids in Section IV-C were generated by taking a fully connected 100 node network and “removing” nodes using scripts that took inputs to an elliptical area and removed all nodes in that area. Two voids are present in both void networks evaluated. To measure the affect of throughput and latency in the network (IV-D), it was not necessary to do a all-to-all flood of the network since that would saturate the network. In

these simulations, 100 connections were formed by randomly selecting a source and destination and sending CBR packets of 512 bytes each for 10 seconds. Latency was measured by taking the difference between the send and receive times of these packets while throughput was calculated by dividing the total bytes received by the total latency. In evaluating delivery success, average path length, total control packets and aggregate throughput in Sections IV-F-IV-H connection patterns were generated in a similar manner by randomly choosing a source and destination. Simulations were run over 10 trials and results averaged with standard deviations given in graphs.

##### B. Affect of Additional Lines on Various Topologies

Section III showed that under differing topologies without any angle correction, connectivity and path stretch is drastically affected by number of lines used for transmissions. It is interesting, therefore, to see how the analysis matches up with packetized simulations with angle correction. We suspected that even with one line, MAM should be able to deal with the majority of perimeter nodes and therefore provide fairly high reachability in symmetric topologies. In asymmetric topologies, however, as the “incident angle” a packet hits a perimeter node becomes steeper, it becomes more difficult to do angle correction since we set a hard limiter to not forward more than  $90^\circ$  to avoid loops so we suspect in these topologies, additional lines will affect reach probability more drastically.

In the same way, because additional lines provide additional paths to choose from, we expect that as the number of lines increase, the average path length from source to destination will decrease. Table IV outlines the simulation parameters that differ from the default and Figure 5 and Figure 6 show our results

TABLE IV  
SIMULATION PARAMETERS: ADDL. LINES ON VARIOUS TOPOLOGIES

Parameter	Values	
TTL for Control Pkts	10	15, 20
Topology Boundaries	300m x 300m	1000m x 200m
Number of Nodes	25, 50, 100	75, 100
Average Number of Neighbors	3.84, 5.04, 10.52	3.6, 5.48

As illustrated in Figure 5, for square topologies, there is a large gain in reach probability going from one line to two lines but the gain thereafter is small even for varying network densities. Average path length, as well, seems to trail off after transmitting orthogonally with two lines. This is expected as even in our analysis, path stretch was close to shortest path even for two lines. In contrast to this, states maintained at each node increased seemingly linearly with increased number of lines. This is expected as more states need to be maintained along linearly increasing number of lines of transmission.

We saw very similar results for rectangular topologies except that the jump from two to three lines provided a larger jump in reach probability. Even with just one line, MAM was able to ensure roughly 67% packet delivery success as compared to the 34.55% shown in our analysis. By increasing the number of lines, additional paths were available despite the

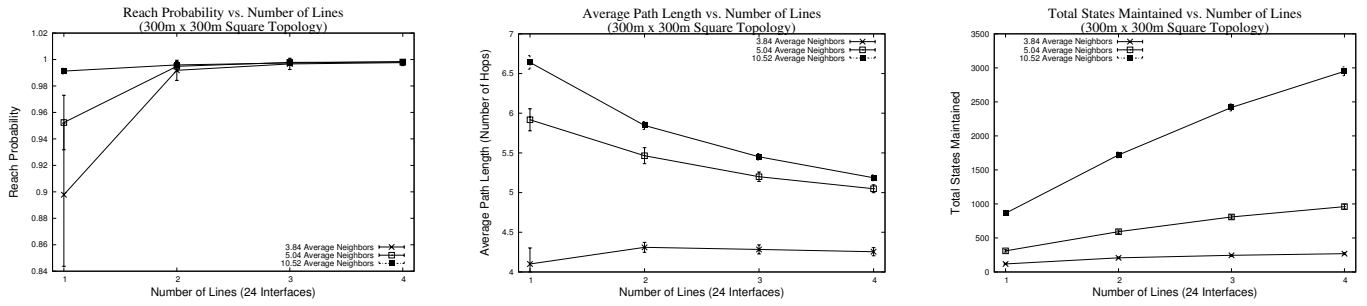


Fig. 5. Reach probability, total states maintained, and average path length vs. number of lines used for transmissions for dense and sparse with no voids present. As expected, as number of lines increased, the reach probability and total states maintained increased while average path length decreased.

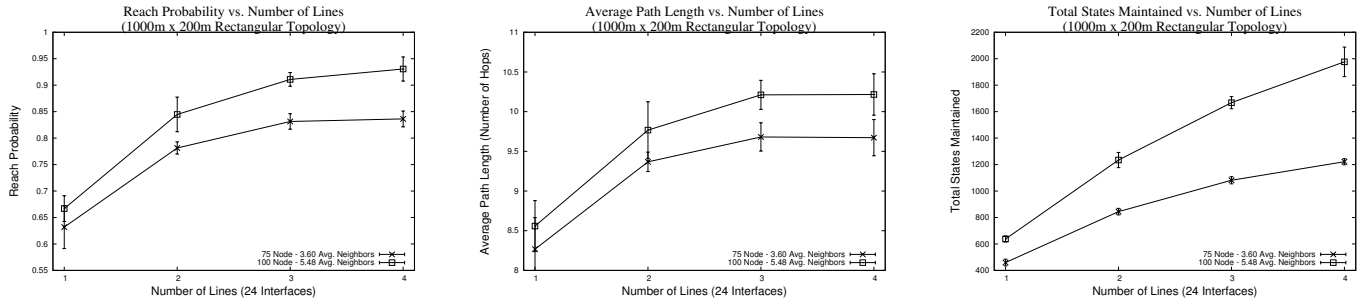


Fig. 6. Reach probability, total states maintained, and average path length vs. number of lines used for a rectangular topology. Reach is drastically affected by additional lines due to better paths in a slim topology.

rather “thin” topology. Figure 6 showed that the average path length curve mimicked the reach probability curve. At first this seems counter intuitive since one would expect that with additional lines and thus, additional paths to choose from, the average path length would be less as lines are increased. However, it is important to note that our simulations only calculate average path length based on *successful* transmissions. Thus, nodes at the edges of the rectangular topology, which would most likely incur the highest number of hops to reach, would be left out if no path is found. This is therefore consistent with our hypothesis and as expected, total states maintained in the network grew fairly linearly with increased number of lines.

#### C. Affect of Number of Lines on Network Voids

It is interesting to see how the number of lines of transmission affect reachability and path length in networks with large voids. We hypothesized that while reach would increase with increased number of lines, average path length would remain fairly constant. This is due to few paths to choose from to navigate around voids and therefore, as long as there is a path, most likely, that path would be the one chosen. Our simulation parameters are listed in Table V.

TABLE V  
SIMULATION PARAMETERS: ADDL. LINES ON NETWORKS WITH VOIDS

Parameter	Values
Number of Nodes	25, 50
Average Number of Neighbors	3.92, 6.2

Figure 7 shows our results for various lines on networks with voids. As expected, the increase from one to two lines yielded a fairly large connectivity gain as well as increased total states maintained network-wide. Average path length, as

expected, remained fairly constant. This was due to relatively few paths to choose from to navigate around voids and therefore fairly consistent path choices were made in the connected network.

#### D. Affect of Number of Lines on Throughput

One of the key metrics in wireless networks is network throughput. In wireless networks, throughput is dependent on a lot of factors like congestion, link quality, etc., which unfortunately become increasingly difficult to simulate. In this section, we try to understand the affect of transmitting along additional lines on aggregate throughput. It is expected that with shorter paths and higher reachability, average throughput network-wide will increase. Table VI gives our simulation parameters and Figure 8 illustrate our results.

TABLE VI  
SIMULATION PARAMETERS: ADDITIONAL LINES ON THROUGHPUT

Parameter	Values
Number of Nodes	100
Average Number of Neighbors	10.52
Number of Random Connections	100
CBR Packet Size	512 KB
Transmission Duration	10.0 seconds

Our results in Figure 8 show that throughput increases with increase in lines. Looking at the reach and average path length graphs, this result is intuitive: with smaller reach probability, packets are not successfully delivered and with higher average path length, the delivery time increases dramatically. In short, the increase in lines of transmission lead to paths that are closer to shortest path, which lead to higher throughput. It is interesting to note that even with higher packet delivery success, higher throughput is not guaranteed.

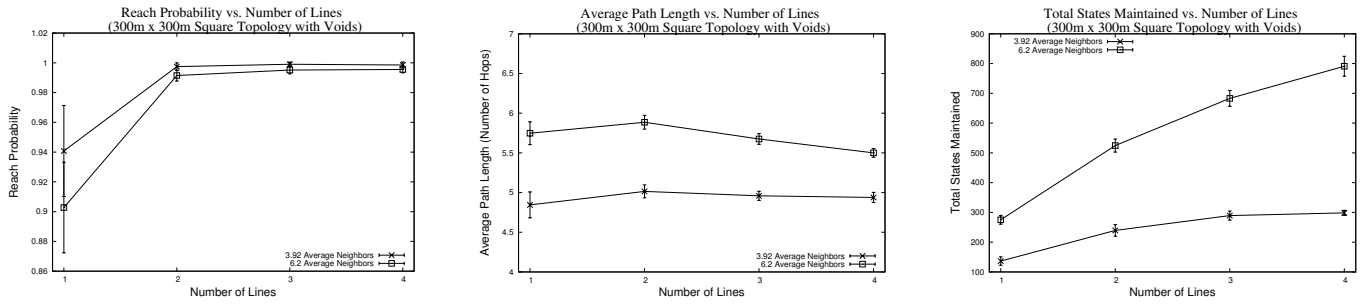


Fig. 7. Reach probability, total states maintained, and average path length vs. number of lines used for transmission for dense and sparse topologies with large voids present. As expected, with voids present, paths taken should be relatively equal due to less choices. At the same time, as more lines are used, the reach probability and total states maintained increased.

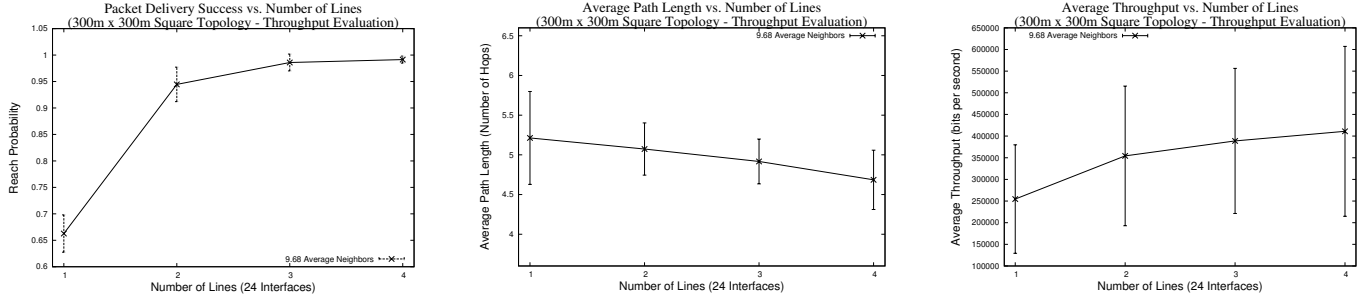


Fig. 8. Average throughput increases as number of lines increase. It can be seen that throughput is largely dependent on average hop count: as average hops increase, the throughput drops.

#### E. Affect of Number of Lines on Varying Network Mobility

Because ORRP was designed primarily for fixed wireless mesh networks, it is expected to fail under mobility because lines cannot be maintained in an efficient manner. Adding additional lines, however, could lead to better paths and increased delivery success even in mobile and/or disruption tolerant environments. In this section, we seek to understand whether addition of lines helps in a mobile environment. We suspect that the addition of lines should *not* affect reach probability much because all paths are moving. Table VII gives our simulation parameters and Figure 9 show our results.

TABLE VII

SIMULATION PARAMETERS: ADDITIONAL LINES ON MOBILE NETWORKS

Parameter	Values
Number of Interfaces	12
Topology Boundaries	300m x 300m
Number of Nodes	100
Mobility	RWP Model: 2.5m/s, 5.0m/s, 7.5m/s
Simulation Time	100s
Connectivity Sampling Frequency	Every 20s

Our results in Figure 9 show that for a mobile network, directional routing protocols like ORRP have severe issues without decreasing the announcement interval and route time-out. However, there seems to be a fairly large increase in reach probability as number of lines increased from 1 to 2 but the gains trail off afterwards. We attribute this increase to having additional and better paths to choose from which in-turn lead to less number of hops and less number of nodes that have moved away providing for a higher reach probability. In the

same way, average path length, as expected, decreased with additional lines as better path options were available.

#### F. Affect of Varying the Number of Interfaces

Adding more interfaces to a node increases the diversity of directions to send with the finer granularity of spread resulting in less neighbors associated with a single interface. It is expected that the gains in delivery success, average path length, and throughput will increase with the number of interfaces up until a point and that this point is determined by the network density. Table VIII lists our simulation parameters that differ from the default and Tables IX-XI give our results. Because it is important to transmit symmetrically (i.e. the angles between each transmission interface must be equal), certain number of interfaces can only transmit along 1, 2, 3 lines while others can only transmit along 1, 2, 4 lines. The N/A values in the tables represent the cases when transmission is not possible.

TABLE VIII

SIMULATION PARAMETERS: AFFECT OF NUMBER OF INTERFACES

Parameter	Values
Number of Nodes	100 (Avg Neighbors: 10.52)
Number of Random Connections	100
CBR Packet Size	512 KB
Transmission Duration	10.0 seconds
Number Interfaces	8, 12, 16, 24
Simulation Time	100s

Table IX shows the packet delivery success for varying number of interfaces and network densities. It can be seen that in general, when number of interfaces increases, there is a large effect on delivery success going from 8 to 12

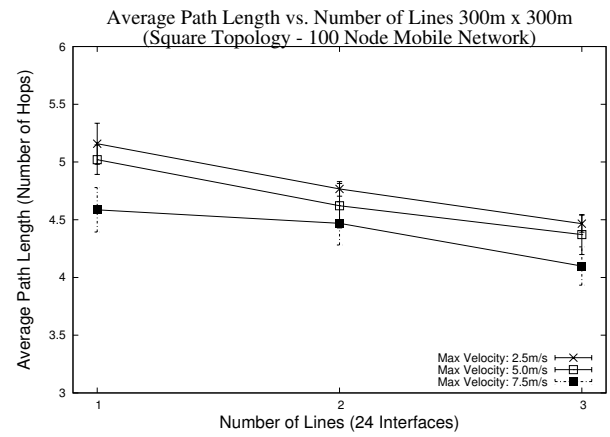
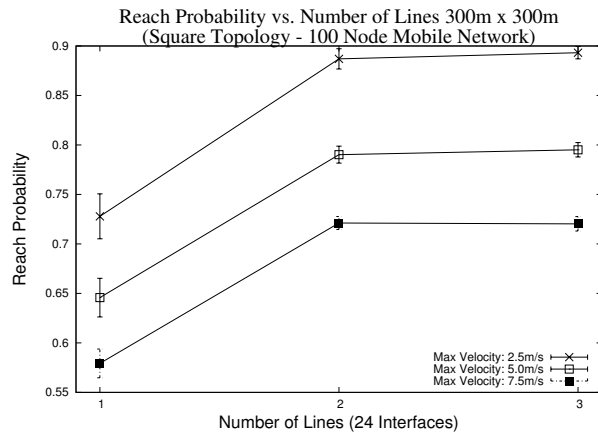


Fig. 9. Reach probability and average path length vs. number of lines used for transmission for mobile networks. ORRP was never designed for mobility but as it can be expected, addition of lines increases reach probability. This is most likely due to shorter paths chosen.

TABLE IX  
DELIVERY SUCCESS VS. NUMBER OF INTERFACES

	1 Line	2 Lines	3 Lines	4 Lines
8 Interfaces (Avg NBs: 9.7)	64.7%	88.3%	N/A	98.0%
8 Interfaces (Avg NBs: 20.9)	65.4%	93.8%	N/A	98.4%
12 Interfaces (Avg NBs: 9.7)	65.3%	93.1%	98.3%	N/A
12 Interfaces (Avg NBs: 20.9)	71.6%	97.3%	99.1%	N/A
16 Interfaces (Avg NBs: 9.7)	65.7%	94.6%	N/A	98.7%
16 Interfaces (Avg NBs: 20.9)	76.4%	98.4%	N/A	99.7%
24 Interfaces (Avg NBs: 9.7)	67.2%	95.6%	99.0%	99.4%
24 Interfaces (Avg NBs: 20.9)	77.2%	99.6%	99.9%	99.9%

interfaces for a network density of 9.7 average neighbors and 12 to 16 for a network density of 20.9 average neighbors. Afterwards, the gains taper off. It is interesting to note that a network density of 9.7 average neighbors per node equates to approximately 1 neighbor per interface. It makes sense that the affect on delivery success would be most affected by the network density as there is approximately one node per network interface. The lower the number of interfaces, the more neighbors are associated with a specific interface and therefore, there is higher risk of announcement and RREQ packets “missing” each other. Additionally, “matching” one neighbor to a specific interface allows MAM to operate to the best efficiency because it can be consistent when choosing random nodes to send to in a specific direction.

TABLE X  
AVERAGE PATH LENGTH (# OF HOPS) VS. NUMBER OF INTERFACES

	1 Line	2 Lines	3 Lines	4 Lines
8 Interfaces (Avg NBs: 9.7)	5.29	5.43	N/A	4.71
8 Interfaces (Avg NBs: 20.9)	6.89	6.12	N/A	5.22
12 Interfaces (Avg NBs: 9.7)	5.35	5.20	4.62	N/A
12 Interfaces (Avg NBs: 20.9)	6.71	6.18	5.34	N/A
16 Interfaces (Avg NBs: 9.7)	5.69	5.13	N/A	4.71
16 Interfaces (Avg NBs: 20.9)	6.56	5.81	N/A	4.48
24 Interfaces (Avg NBs: 9.7)	5.18	5.21	4.80	4.44
24 Interfaces (Avg NBs: 20.9)	6.28	5.50	4.64	4.44

As can be seen from Table X, as number of interfaces increase, the average path length generally decreases. The affect is more noticeable with denser networks and more

lines as having more interfaces increases the granularity of neighbors associated with a specific interface. This refines the neighbor selection and allows for better paths. Because increase in node density leads to *shorter* distances to neighbors and *more* hops to go from source to destination, it makes sense that with *less* interfaces (more neighbors associated with a specific interface), paths chosen would be worse.

TABLE XI  
THROUGHPUT (KBPS) VS. NUMBER OF INTERFACES

	1 Line	2 Lines	3 Lines	4 Lines
8 Interfaces (Avg NBs: 9.7)	71.2	92.7	N/A	200.5
8 Interfaces (Avg NBs: 20.9)	44.0	77.1	N/A	155.9
12 Interfaces (Avg NBs: 9.7)	130.4	181.4	321.0	N/A
12 Interfaces (Avg NBs: 20.9)	60.5	135.1	246.7	N/A
16 Interfaces (Avg NBs: 9.7)	144.0	187.5	N/A	387.0
16 Interfaces (Avg NBs: 20.9)	79.0	192.8	N/A	508.4
24 Interfaces (Avg NBs: 9.7)	213.9	300.8	407.7	503.2
24 Interfaces (Avg NBs: 20.9)	123.6	453.6	723.4	666.9

Table XI shows the throughput vs. number of interfaces. It can be seen that throughput for denser networks is generally smaller for the same number of interfaces because denser networks incur additional hops from source to destination. However, as number of interfaces and number of lines increase, it seems that throughput becomes much better with denser networks. We suspect this is not only due to better paths, but also less interference between transmissions as more interfaces localize affected nodes better.

#### G. Network Density Evaluation vs. AODV and DSR

It is interesting to understand how network density affects packet delivery success, average path length, total control packets, and average throughput network-wide for ORRP with multiple lines compared to other routing protocols like AODV and DSR. It is expected that with broadcast protocols that use omni-directional antennas such as AODV and DSR, as density increases, less packets will be delivered resulting in lower throughput. Table XII gives the simulation parameters which differ from the default and Figures 10 and 11 show our results.



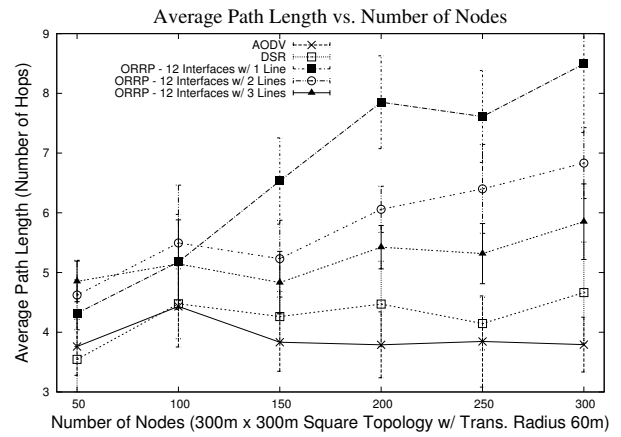
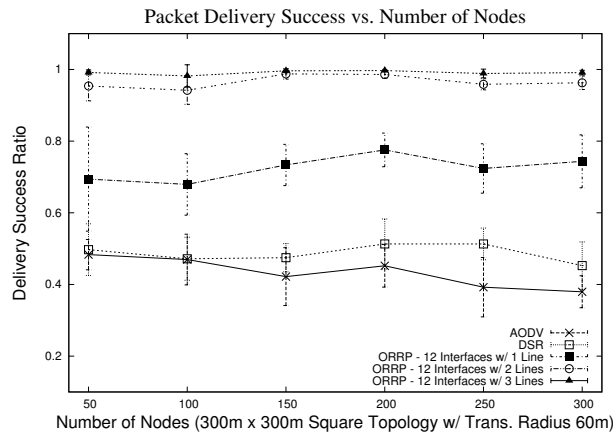


Fig. 10. Packet delivery success and average path length vs. number of nodes in the network for various routing protocols. It can be seen that with more lines, ORRP delivers more packets with shorter average path length. Because AODV and DSR utilize shortest path algorithms, it is expected that average path length is smaller compared to ORRP.

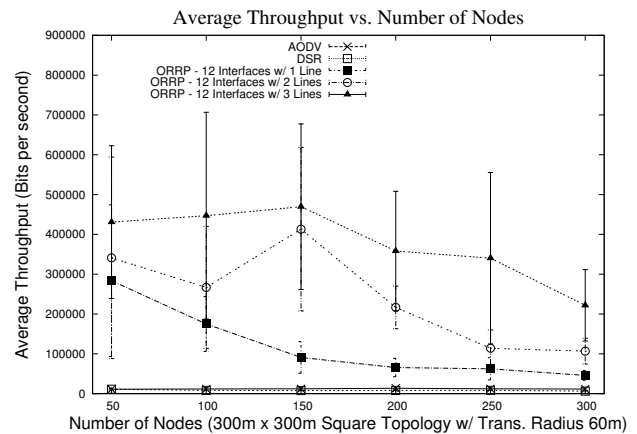
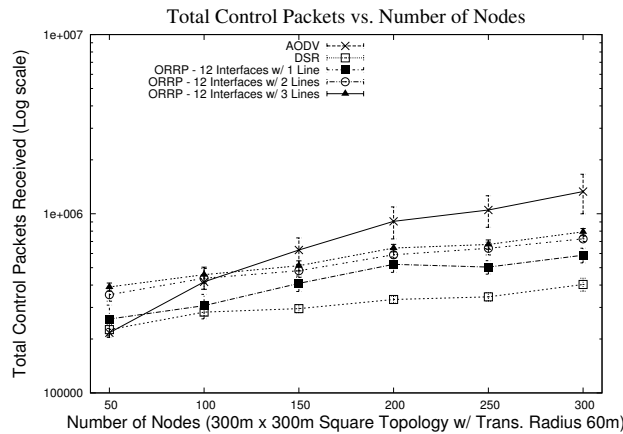


Fig. 11. Control packets received and average throughput vs. number of nodes in the network for various routing protocols. ORRP with more lines sends out more control packets as expected. Because ORRP is a hybrid proactive/reactive protocol, it is expected to disseminate more packets than DSR and AODV. Throughput is very much dependent on average path length.

TABLE XII

SIMULATION PARAMETERS: NETWORK DENSITY EVALUATION VS. AODV AND DSR

Parameter	Values
Number of Interfaces	12
Topology Boundaries	300m x 300m
Number of Nodes	50, 100, 150, 200, 250, 300
Avg. # of Neighbors	5.1, 9.7, 15.6, 20.9, 26.1, 29.7
Simulation Time	100s
Connection Pattern	50 Random Connections - 10s each
TTL for Control Pkts	15
Simulation Time	100s

As can be seen from Figure 10, as network density (number of nodes) is increased, ORRP maintains fairly consistent high delivery success while AODV and DSR steadily decline. Even with smaller density, with 50 random connections, the network becomes quickly saturated with omnidirectional communications methods. As expected, ORRP with one line yields the highest average path length as having only 1 intersection point results in longer paths. As more lines are introduced, the average path length declines steadily. Because AODV and DSR use shortest path algorithms for route discovery, it is expected that

they yield the smallest average path length even despite packet losses. Figure 11 shows that with increased network density (number of nodes), ORRP requires relatively the same amount of control packets as DSR and AODV. Even though ORRP has a proactive element that disseminates packets periodically, it still is able to maintain a relatively competitive number of control packets because of its directional nature. As expected, with increased lines, more control packets are required to be sent. Average throughput is affected mostly by the average path length graph with smaller number of hops equating to better throughput for the case of ORRP. In the case of DSR and AODV, network saturation with omnidirectional antennas prevents packets from being successfully distributed resulting in low throughput.

#### H. Number of Connections Evaluation vs. AODV and DSR

It has been shown that network congestion can be controlled and limited by routing packets using two-phase routing algorithms [26] [25]. Current wireless networks measure route cost through hop count. In high-traffic networks, by choosing the shortest path, nodes with many connections will become



saturated with packets. [26] has shown that by drawing a perpendicular bisector between source and destination and forwarding packets from source to a random point on the perpendicular bisector which in-turn forwards to destination when that point is reached, load can be balanced across the network. In much the same way, ORRP inherently implements a seemingly two-phase routing algorithm because it provides rendezvous abstractions whereby the source sends to the rendezvous node and the rendezvous node sends to the destination. In this section, we seek to understand how the number of connections affect the packet delivery success, average path length, control packets, and average throughput network-wide with ORRP, AODV, and DSR. Table XIII gives the simulation parameters that differ from the default.

TABLE XIII  
SIMULATION PARAMETERS: NETWORK OF CONNECTIONS EVALUATION  
VS. AODV AND DSR

Parameter	Values
Number of Interfaces	12
Topology Boundaries	300m x 300m
Number of Nodes	100 (Avg # Neighbors: 9.68)
Simulation Time	100s
Connection Pattern	10-100 Random Connections - 10s each
TTL for Control Pkts	15
Simulation Time	100s

As can be seen from Figure 12, ORRP with more lines delivers far more packets than AODV or DSR and is fairly consistent in number of packets delivered despite number of connections. This is due to more efficient medium usage by directional communications methods. AODV and DSR suffer when the network becomes more saturated. Average path length for all cases seems fairly constant as number of connections shouldn't affect the path length chosen. Figure 13 shows that the total control packets received increases with number of connections. This is expected as ORRP, DSR, and AODV all have a reactive element to it - as more packets need to be sent, more route requests need to be performed. Average throughput drops with more connections and congestion in the network because packets are in queues longer.

## V. FUTURE WORK AND CONCLUSION

In this paper, we extended Orthogonal Rendezvous Routing Protocol (ORRP) to send packets out additional directions to measure the tradeoff between delivery success, average path length, total states maintained, and aggregate throughput. Our analysis in section III showed that the jump between one line and two lines yields significant increases in reach probability and path stretch while the addition of more lines gives only *marginal gains* in reach probability but should choose much better paths resulting in smaller path stretch. Because the numerical analysis was performed with straight line paths without angle correction deviations, packetized simulations were necessary.

We simulated the affect of number of lines of transmission had on reach probability, average path length, total states maintained network-wide, control packet overhead and aggregate throughput on various topologies, network densities,

void conditions, number of connections, number of interfaces, and mobility. Our results indicated that in non-void, non-mobile scenarios, there is a significant increase in delivery success and throughput from one to two lines but as suggested by our analysis, the gains after adding additional lines are slim. Average path length was also shown to decrease until shortest path was almost reached in increasing number of lines. Additionally, as the number of lines increased, total states maintained in the network increased fairly linearly (but still order  $N^{3/2}$ ). As voids were added, however, average path length remained fairly constant due to similar paths taken despite seemingly more paths to choose from. With mobility, it was shown that the addition of lines had very little affect on delivery success but dropped average path length marginally as expected.

Overall, the addition of lines yields only marginal gains over the two orthogonal lines scenario suggested in [1] and it would be interesting to explore additional methods for deviation correction, perimeter routing, and void traversals to account for the few percentage of unsuccessful packets delivered. Furthermore, since ORRP fails drastically in mobile environments even with decreased announcement intervals and route lifetime, it would be interesting to look at the possibility of extending ORRP to mobile adhoc networks.

## REFERENCES

- [1] Bow-Nan Cheng, Murat Yuksel, Shivkumar Kalyanaraman, "Orthogonal Rendezvous Routing Protocol for Wireless Mesh Networks," Proceedings of the 17th IEEE International Conference on Network Protocols (ICNP), November 2006.
- [2] Bow-Nan Cheng, Murat Yuksel, Shivkumar Kalyanaraman, "Directional Routing for Wireless Mesh Networks: A Performance Evaluation," To appear in the Proceedings of IEEE Workshop on Local and Metropolitan Area Networks (LANMAN), Princeton, NJ, June 2007.
- [3] Hrishikesh Gossain, Tarun Joshi, Carlos De Moraes Cordeiro, and Dharma P. Agrawal, "DRP: An Efficient Directional Routing Protocol for Mobile Ad Hoc Networks," IEEE Trans. Parallel and Distributed Systems, vol. 17, no. 12, 2006, pp. 1439-1451.
- [4] B. Karp and H.T. Kung, "GPSR: Greedy Perimeter Stateless Routing for Wireless Networks," Proceedings of ACM/IEEE MOBICOM, Boston, MA, August 2000.
- [5] J. Li, J. Jannotti, D.S.J. De Couto, D.R. Karger, and R. Morris, "A Scalable Location Service for Geographic Ad Hoc Routing," Proceedings of ACM/IEEE MOBICOM, pp. 120-130, Aug. 2000.
- [6] John Bicket, Daniel Aguayo, Sanjit Biswas, and Robert Morris, Architecture and Evaluation of an Unplanned 802.11b Mesh Network, *ACM/IEEE MOBICOM* 2005.
- [7] Charles Perkins and Pravin Bhagwat, Highly Dynamic Destination-Sequenced Distance-Vector Routing (DSDV) for Mobile Computers. Proceedings of ACM SIGCOMM, pages 234-244, 1994.
- [8] Charles E. Perkins and Elizabeth M. Royer. "Ad hoc On-Demand Distance Vector Routing." Proceedings of the 2nd IEEE Workshop on Mobile Computing Systems and Applications, New Orleans, LA, February 1999, pp. 90-100.
- [9] David B. Johnson, David A. Maltz, Josh Broch. DSR: The Dynamic Source Routing Protocol for Multi-Hop Wireless Ad Hoc Networks. *Ad Hoc Networking*, edited by Charles E. Perkins, Chapter 5, pp. 139-172, Addison-Wesley, 2001.
- [10] T. Clausen and P. Jacquet. OLSR RFC3626, October 2003. <http://ietf.org/rfc/rfc3626.txt>.
- [11] W. T. Tsai , C. V. Ramamoorthy , W. K. Tsai, O. Nishiguchi, An Adaptive Hierarchical Routing Protocol, *IEEE Transactions on Computers*, v.38 n.8, p.1059-1075, August 1989.

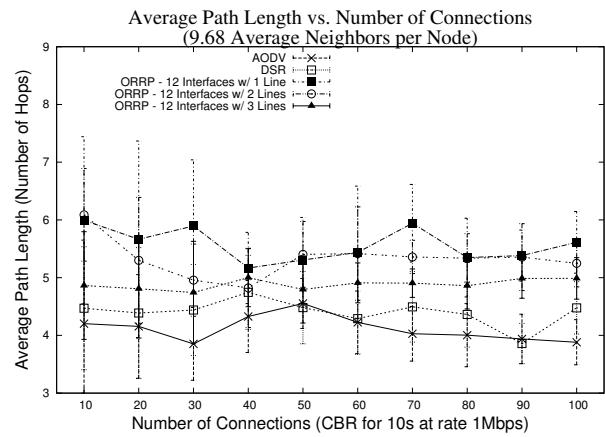
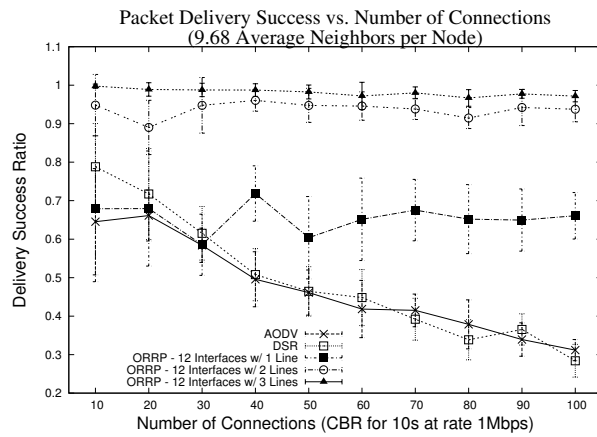


Fig. 12. Data delivery success and average path length vs. number of connections. As connections increase, it can be seen that the network becomes saturated faster with AODV and DSR. Average path length is fairly constant throughout.

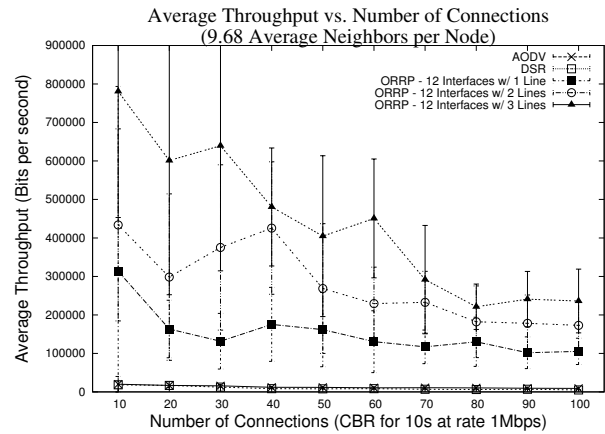
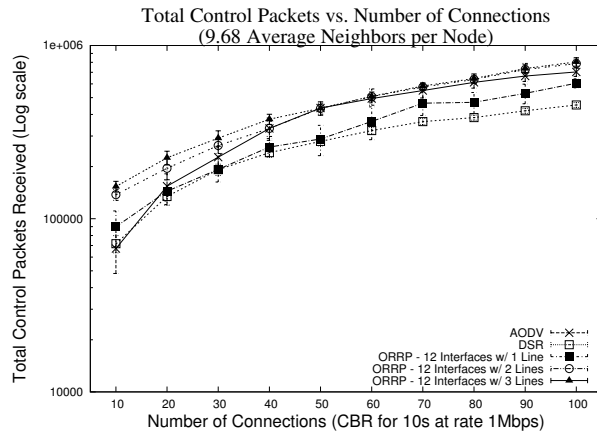


Fig. 13. Total control packets received and average throughput vs. number of connections. With more connections, more control packets and congestion result in throughput drops.

- [12] Romit Roy Choudhury and Nitin Vaidya. "Impact of Directional Antennas on Ad Hoc Routing", Proceedings of the Eighth International Conference on Personal Wireless Communication (PWC), Venice, September 2003.
- [13] R. Ramanathan. "On the performance of ad hoc networks using beam-forming antennas", Proceedings of ACM MOBIHOC, October 2001.
- [14] Su Yi, Yong Pei, and Shivkumar Kalyanaraman, "On the Capacity Improvement of Ad Hoc Wireless Networks Using Directional Antennas," Proceedings of ACM MOBIHOC, Pages 108-116, Annapolis, MD, June 2003.
- [15] Jayasri Akella, Chang Liu, David Partyka, Murat Yuksel, Shiv Kalyanaraman, and Partha Dutta, "Building Blocks for Mobile Free-Space-Optical Networks," Proceedings of IFIP/IEEE WOCN, pages 164-168, Dubai, United Arab Emirates, March 2005.
- [16] D. Braginsky and D. Estrin, "Rumor routing algorithm for sensor networks," Proceedings of WSN, Atlanta, GA, October 2002.
- [17] The Network Simulator. ns-2. <http://www.isi.edu/nsnam/ns>.
- [18] Romit Roy Choudhury, Nitin H. Vaidya "Performance of Ad Hoc Routing using Directional Antennas" Journal of Ad Hoc Networks - Elsevier Publishers, November, 2004.
- [19] Amit Kumar Saha and David B. Johnson. Routing Improvements Using Directional Antennas in Mobile Ad Hoc Networks. IEEE Globecom, Dallas, Texas, November 2004.
- [20] S. Ratnasamy, B. Karp, L. Yin, F. Yu, D. Estrin, R. Govindan, and S. Shenker, "GHT: A geographic hash table for data-centric storage in sensor networks," In Proceedings of the First ACM International Workshop on Wireless Sensor Networks and Applications (WSNA) 2002.
- [21] S. Kalyanaraman S. Yi, Y. Pei and B. Azimi-Sadjadi, "How is the capacity of ad hoc networks improved with directional antennas," Accepted for Publication in Wireless Networks, 2005.
- [22] R. R. Choudhury, X. Yang, R. Ramanathan and N. H. Vaidya, "Using Directional Antennas for Medium Access Control in Ad Hoc Networks," In Proceedings of MobiCom, pp. 59-70, Sep. 2002.
- [23] H. Willebrand and B. S. Ghuman, Free Space Optics (Sams Pubs, 1st edition, 2001).
- [24] D. J. T. Heatley, D. R. Wisely, I. Neild, and P. Cochrane, Optical Wireless: The story so far, IEEE Communications (December 1998), Volume 36, pp. 72 - 74.
- [25] M. Kodialam, T. V. Lakshman, and Sudipta Sengupta, "Efficient and Robust Routing of Highly Variable Traffic", Third Workshop on Hot Topics in Networks (HotNets-III), San Diego (USA), November 2004.
- [26] Costas Busch, Malik-Magdon Ismail, and Jing Xi, "Oblivious Routing on Geometric Networks", Proceedings of the 17th ACM Symposium on Parallelism in Algorithms and Architectures (SPAA), pp 316-324, Las Vegas, Nevada, July 2005.